

Reg. No. :

M 11867

Name :

Fourth Semester M.Sc. Degree Examination, May 2006

PHYSICS

PH-401 : Statistical Mechanics

(2004 Admn.)

Time: 3 Hours

Max. Marks: 80

Instruction : Answer all questions.

PART – A

Essay questions – $3 \times 12 = 36$ marks :

1. a) Derive Bose-Einstein distribution law.
b) How would it be used to obtain Plank's formula for the black body radiation ? 12
 2. What is Fermi gas ? Deduce an expression for the energy of a Fermi gas at absolute zero. Point out its physical significance. 12
 3. Define grand partition function. How can you obtain various thermodynamic quantities from it ? Discuss density fluctuations in grand canonical ensemble. 12
- $3 \times 12 = 36$

PART – B

Short answer questions – $7 \times 5 = 35$ marks :

4. What is Gibb's paradox ? How it can be resolved ? 5
5. What do you mean by the terms phase space and ensembles ? 5
6. Define density matrix for various thermodynamic parameters from the density operator. 5
7. Briefly explain equipartition theorem. 5

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8. Show that the entropy at absolute zero in a canonical ensemble can be expressed as $s = K \log g_0$ where g_0 is the statistical weight of the ground state. 5
9. Discuss free electron theory for metals. 5
10. Explain how Ising model can simulate lattice gas. 5

7×5=35

PART - C

Problem type questions - 4×8=32 marks :

11. Consider that white dwarf is an electron gas of density 10^{30} electrons per cm^3 . Calculate the Fermi energy of the system and the corresponding Fermi temperature.
12. Show that $\mu = -\frac{KT}{N}$ as $T \rightarrow 0$ for a Bose-Einstein gas with ground state at $\epsilon = 0$. 8
13. Using Heisenberg's uncertainty relation $\Delta p \cdot \Delta q \leq \frac{h}{2}$, show that the volume occupied by each energy state in Gamma space is $\left(\frac{h}{2}\right)^{3N}$.
14. Show that the probability that a system in equilibrium with a heat reservoir at temperature T may exist in a microstate of energy ϵ_r is proportional to $\exp\left(-\frac{\epsilon_r}{KT}\right)$ where K is Boltzmann's constant. 4×8=32